

Online Computation of Euclidean Shortest Paths in Two Dimensions

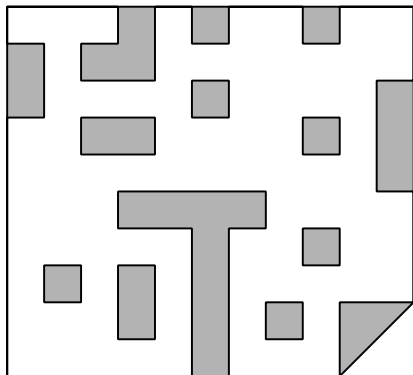
ICAPS 2020

Ryan Hechenberger, Peter J Stuckey, Daniel Harabor,
Pierre Le Bodic, Muhammad Aamir Cheema

Monash University

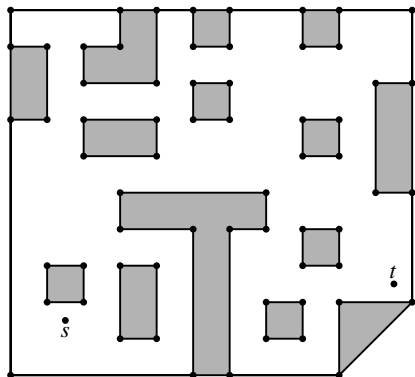
Euclidean Shortest Path

- ▶ Pathfinding on the Euclidean plane



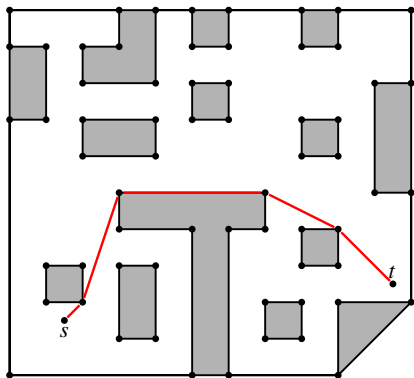
Euclidean Shortest Path

- ▶ Pathfinding on the Euclidean plane
- ▶ Takes as input start s , target t and a set of polygonal obstacles P



Euclidean Shortest Path

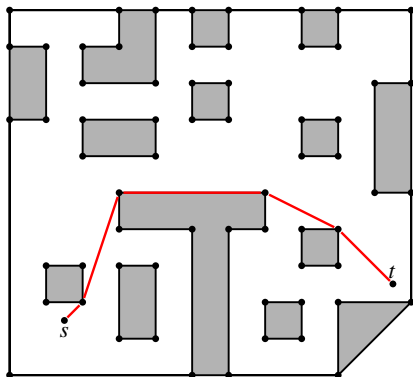
- ▶ Pathfinding on the Euclidean plane
- ▶ Takes as input start s , target t and a set of polygonal obstacles P
- ▶ Find shortest path from s to t without crossing through any obstacles P



Euclidean Shortest Path

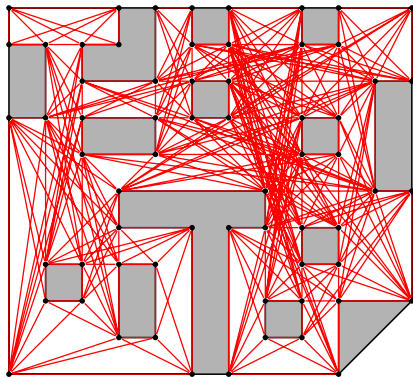
- ▶ Pathfinding on the Euclidean plane
- ▶ Takes as input start s , target t and a set of polygonal obstacles P
- ▶ Find shortest path from s to t without crossing through any obstacles P
- ▶ Distance is based off the Euclidean distance

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



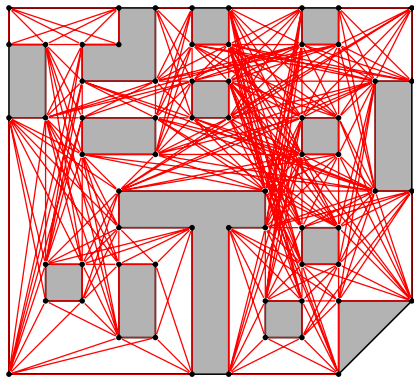
Visibility Graph

- ▶ Visibility graphs can solve the Euclidean shortest path (Lozano-Pérez et al. 1979)



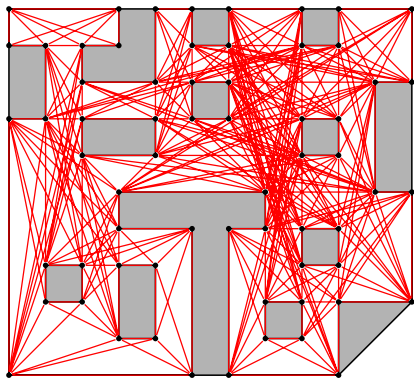
Visibility Graph

- ▶ Visibility graphs can solve the Euclidean shortest path (Lozano-Pérez et al. 1979)
- ▶ Generates graph $G = (V, E)$ where V is polygon vertices and E is edges that are free of all obstacles



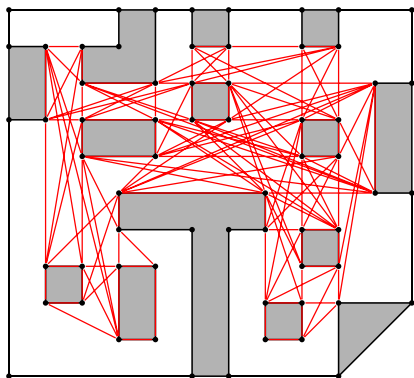
Visibility Graph

- ▶ Visibility graphs can solve the Euclidean shortest path (Lozano-Pérez et al. 1979)
- ▶ Generates graph $G = (V, E)$ where V is polygon vertices and E is edges that are free of all obstacles
- ▶ A full visibility graph uses V^2 edges complexity



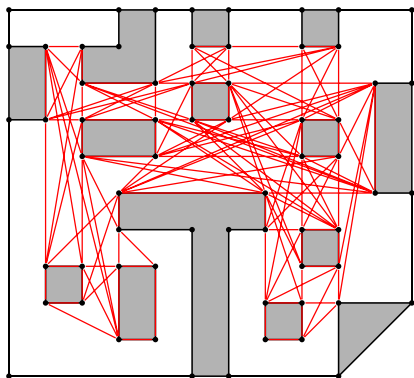
Sparse Visibility Graph

- ▶ A variant of the visibility graph (Oh et al., SoCS 2017)



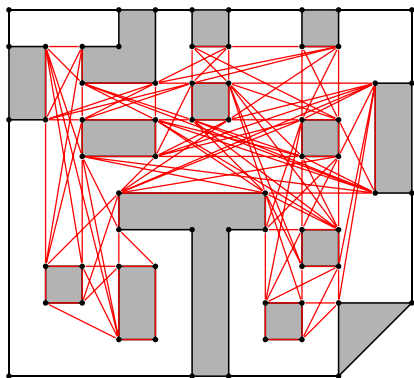
Sparse Visibility Graph

- ▶ A variant of the visibility graph (Oh et al., SoCS 2017)
- ▶ Keeps only edges that can form a shortest path



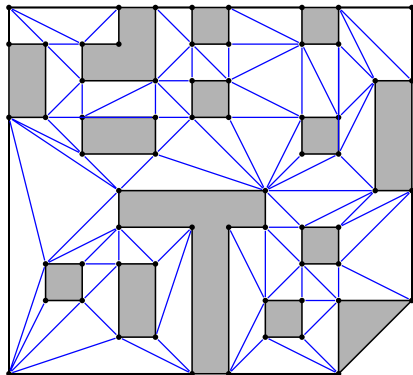
Sparse Visibility Graph

- ▶ A variant of the visibility graph (Oh et al., SoCS 2017)
- ▶ Keeps only edges that can form a shortest path
- ▶ Greatly reduces the density of edges



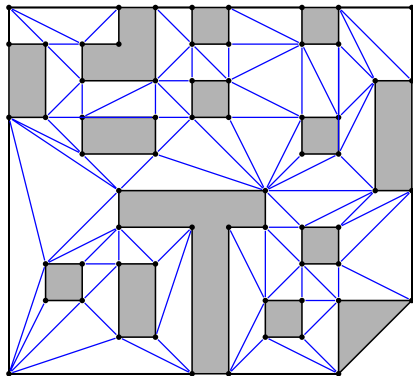
Navigation Mesh

- ▶ Inverts the search space from a set of non-traversable obstacles to traversable convex regions



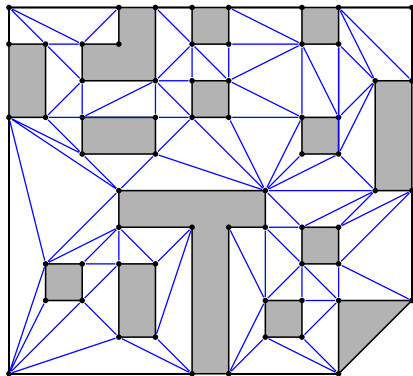
Navigation Mesh

- ▶ Inverts the search space from a set of non-traversable obstacles to traversable convex regions
- ▶ Has a state-of-the-art solver Polyanya (Cui et al., IJCAI 2017)



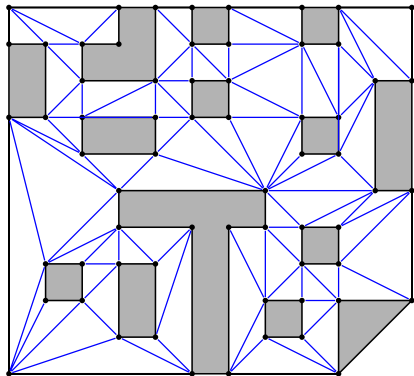
Navigation Mesh

- ▶ Inverts the search space from a set of non-traversable obstacles to traversable convex regions
- ▶ Has a state-of-the-art solver Polyanya (Cui et al., IJCAI 2017)
- ▶ Requires less memory and are easier to construct than visibility graphs



Navigation Mesh

- ▶ Inverts the search space from a set of non-traversable obstacles to traversable convex regions
- ▶ Has a state-of-the-art solver Polyanya (Cui et al., IJCAI 2017)
- ▶ Requires less memory and are easier to construct than visibility graphs
- ▶ Like visibility graphs, does not solve the problem directly



Introducing RayScan

- ▶ An online method for solving the Euclidean shortest path

Introducing RayScan

- ▶ An online method for solving the Euclidean shortest path
- ▶ Works as an on-the-fly partial visibility graph on a A* search

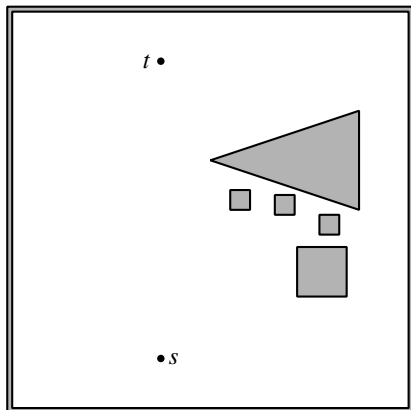
Introducing RayScan

- ▶ An online method for solving the Euclidean shortest path
- ▶ Works as an on-the-fly partial visibility graph on a A^* search
- ▶ Generates edges for each expanding node; they can be discarded after being pushed to the priority queue

RayScan Concepts

Shooting Rays Direct the Search

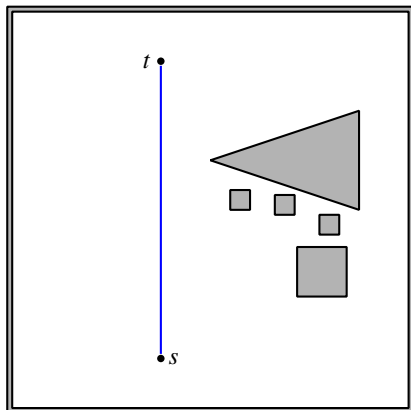
- ▶ Expand start node s



RayScan Concepts

Shooting Rays Direct the Search

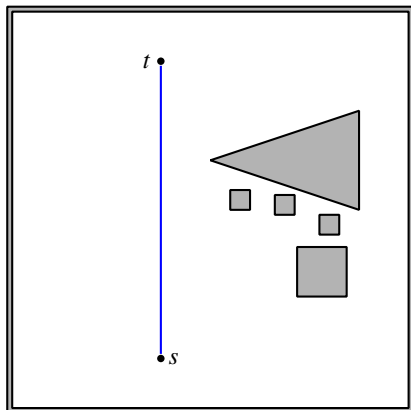
- ▶ Expand start node s
- ▶ Shoot a ray towards target point t



RayScan Concepts

Shooting Rays Direct the Search

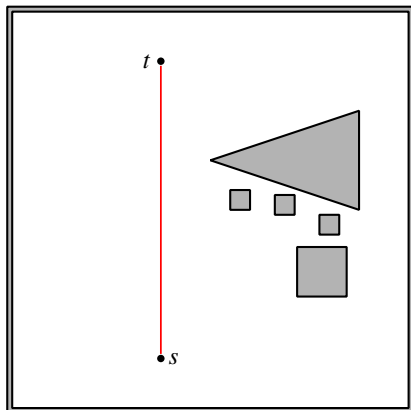
- ▶ Expand start node s
- ▶ Shoot a ray towards target point t
- ▶ If point is visible, it is a successor



RayScan Concepts

Shooting Rays Direct the Search

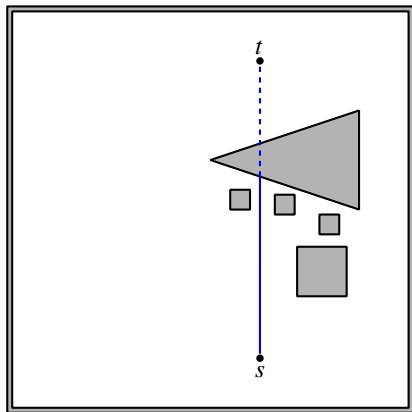
- ▶ Expand start node s
- ▶ Shoot a ray towards target point t
- ▶ If point is visible, it is a successor
- ▶ Direct line-of-sight from s to t is the simplest case



RayScan Concepts

Scanning

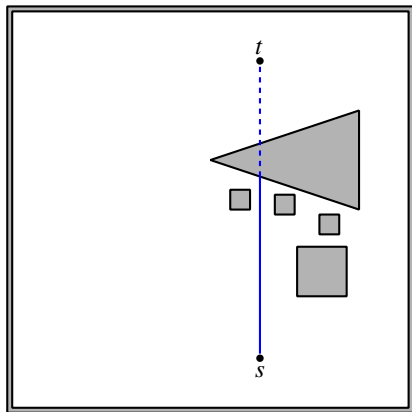
- ▶ Target t is not visible from start s



RayScan Concepts

Scanning

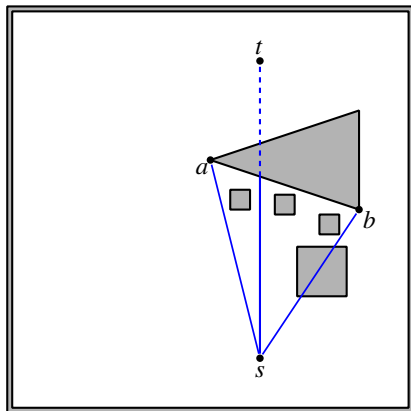
- ▶ Target t is not visible from start s
- ▶ First obstacle blocking target needs to be navigated around



RayScan Concepts

Scanning

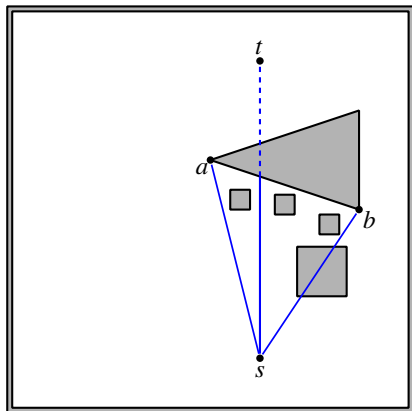
- ▶ Target t is not visible from start s
- ▶ First obstacle blocking target needs to be navigated around
- ▶ Scanning is a core concept to find methods of navigating around obstruction



RayScan Concepts

Scanning

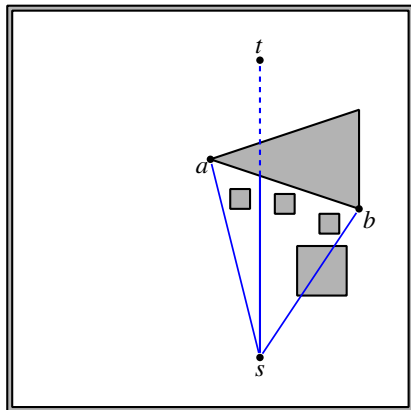
- ▶ Target t is not visible from start s
- ▶ First obstacle blocking target needs to be navigated around
- ▶ Scanning is a core concept to find methods of navigating around obstruction
- ▶ Find turning point a and b scanning CCW/CW that we can bend around



RayScan Concepts

Recursion

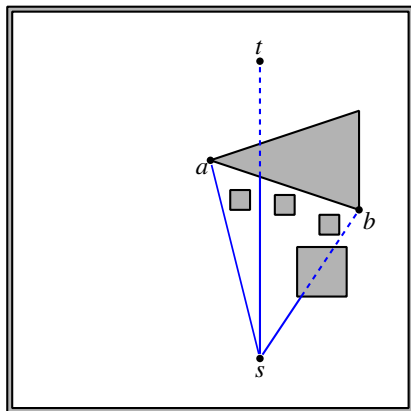
- ▶ Turning point a is visible from s



RayScan Concepts

Recursion

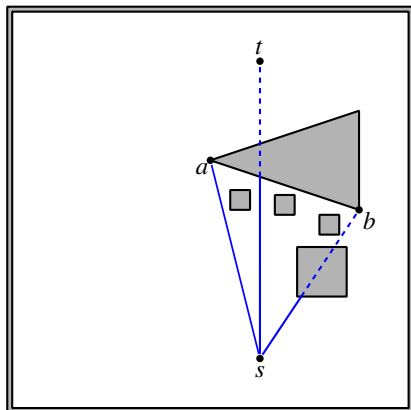
- ▶ Turning point a is visible from s
- ▶ Turning point b is blocked from s



RayScan Concepts

Recursion

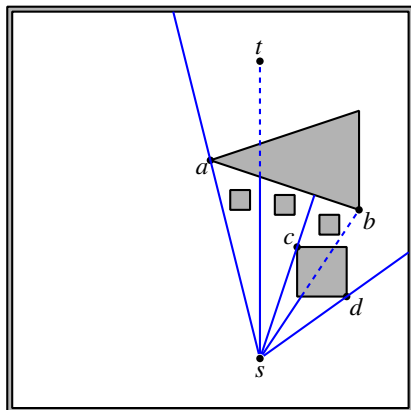
- ▶ Turning point a is visible from s
- ▶ Turning point b is blocked from s
- ▶ The ray shot to b directs the search to find successors that may lead to it



RayScan Concepts

Recursion

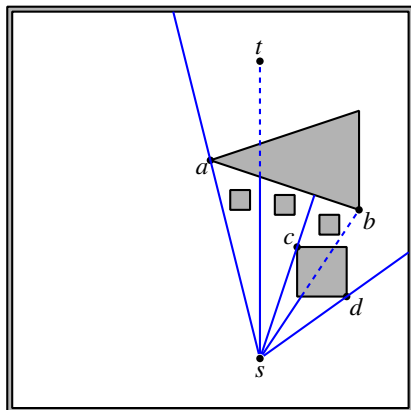
- ▶ Turning point a is visible from s
- ▶ Turning point b is blocked from s
- ▶ The ray shot to b directs the search to find successors that may lead to it
- ▶ Recurse the scan CCW/CW from obstruction intersection



RayScan Concepts

Recursion

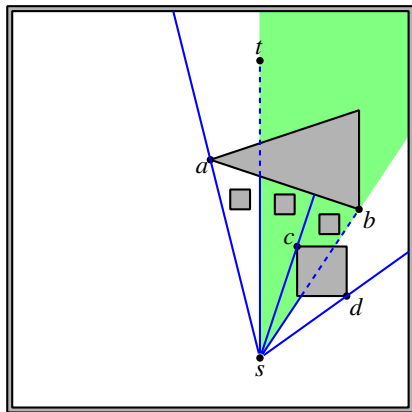
- ▶ Turning point a is visible from s
- ▶ Turning point b is blocked from s
- ▶ The ray shot to b directs the search to find successors that may lead to it
- ▶ Recurse the scan CCW/CW from obstruction intersection
- ▶ Successors c and d is found



RayScan Concepts

Angled Sectors

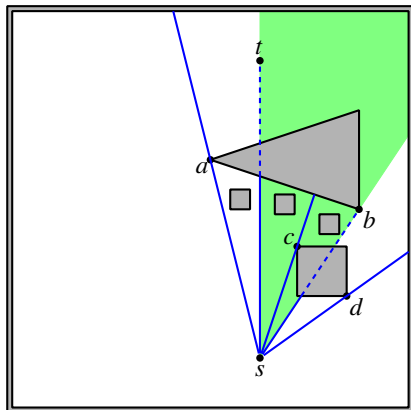
- Scan is restricted to a region called the angled sector



RayScan Concepts

Angled Sectors

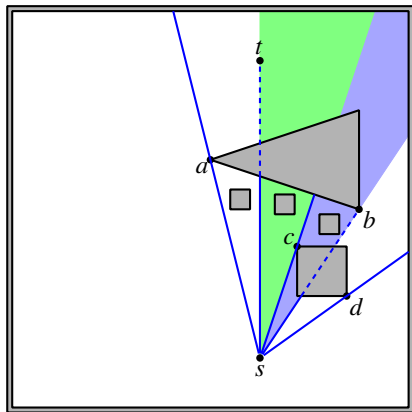
- ▶ Scan is restricted to a region called the angled sector
- ▶ Once the scan leaves the angled sector, it ends



RayScan Concepts

Angled Sectors

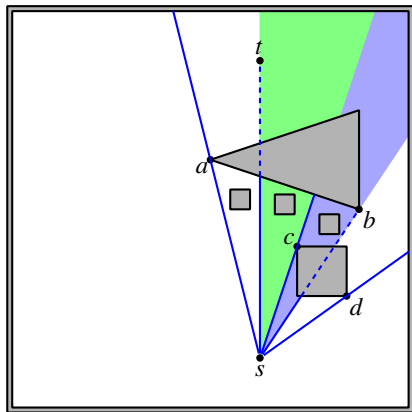
- ▶ Scan is restricted to a region called the angled sector
- ▶ Once the scan leaves the angled sector, it ends
- ▶ When recursing a scan CW/CCW, angled sector is also split



RayScan Concepts

Angled Sectors

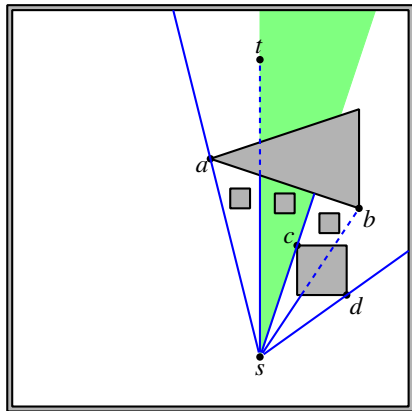
- ▶ Scan is restricted to a region called the angled sector
- ▶ Once the scan leaves the angled sector, it ends
- ▶ When recursing a scan CW/CCW, angled sector is also split
- ▶ After finding c , the angled sector gets splits



RayScan Concepts

Angled Sectors

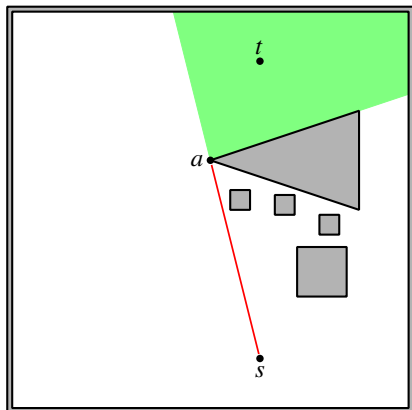
- ▶ Scan is restricted to a region called the angled sector
- ▶ Once the scan leaves the angled sector, it ends
- ▶ When recursing a scan CW/CCW, angled sector is also split
- ▶ After finding c , the angled sector gets splits
- ▶ The CCW scan uses the green split



RayScan Concepts

Next Expansion

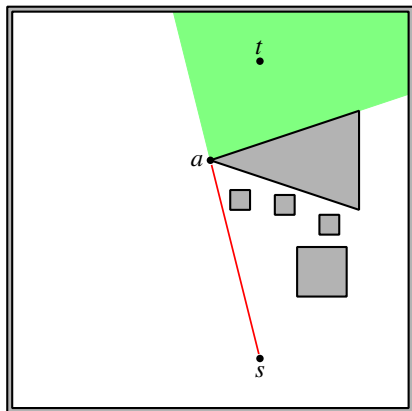
- ▶ A* search expands the smallest f -value a



RayScan Concepts

Next Expansion

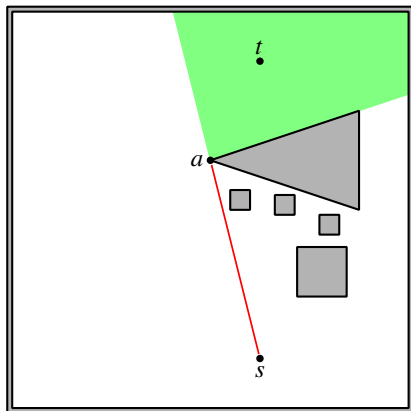
- ▶ A* search expands the smallest f -value a
- ▶ Each expanding node has a special angled sector known as the projection field



RayScan Concepts

Next Expansion

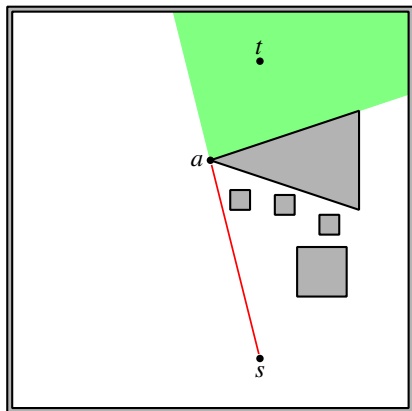
- ▶ A* search expands the smallest f -value a
- ▶ Each expanding node has a special angled sector known as the projection field
- ▶ All successor must fall within this field to ensure taut (bends around corner)



RayScan Concepts

End Search

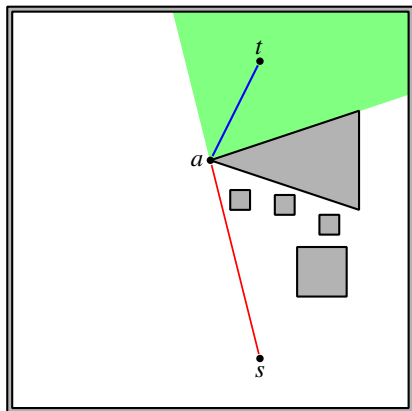
- ▶ Expanding a , target t is within the projection field



RayScan Concepts

End Search

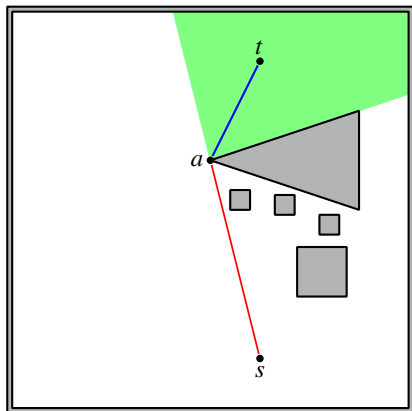
- ▶ Expanding a , target t is within the projection field
- ▶ Shoot ray to t



RayScan Concepts

End Search

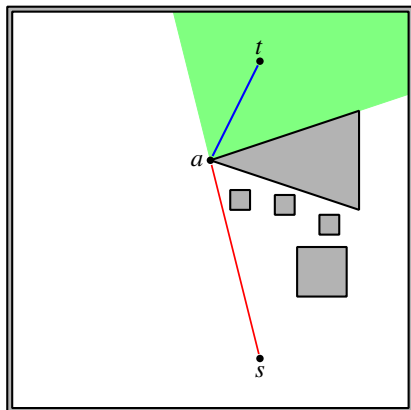
- ▶ Expanding a , target t is within the projection field
- ▶ Shoot ray to t
- ▶ Target is visible, successor is added



RayScan Concepts

End Search

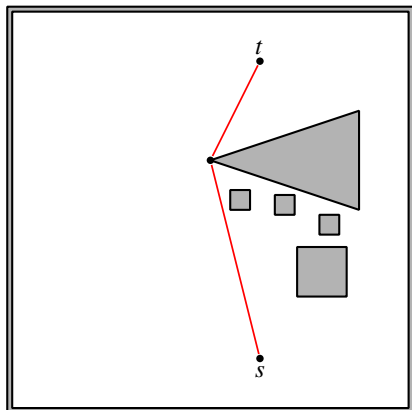
- ▶ Expanding a , target t is within the projection field
- ▶ Shoot ray to t
- ▶ Target is visible, successor is added
- ▶ Expansion of node ends since target is found



RayScan Concepts

End Search

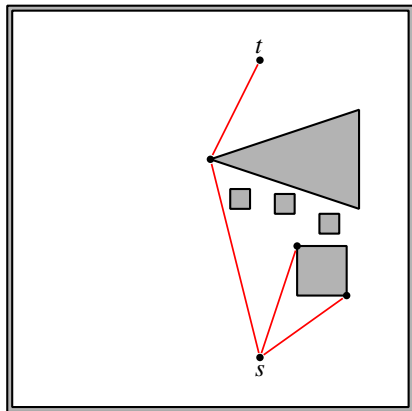
- ▶ Expanding a , target t is within the projection field
- ▶ Shoot ray to t
- ▶ Target is visible, successor is added
- ▶ Expansion of node ends since target is found
- ▶ If using a Euclidean heuristic value, search ends here



RayScan Concepts

Skipped Successors

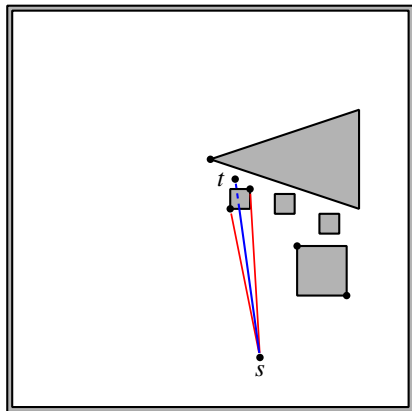
- ▶ Multiple squares are not considered



RayScan Concepts

Skipped Successors

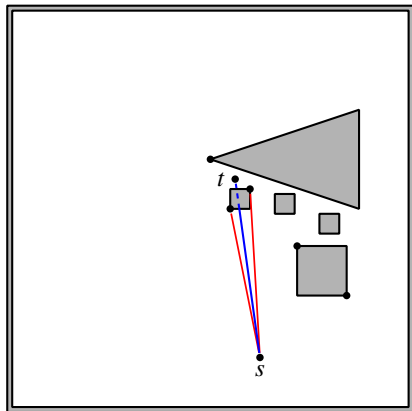
- ▶ Multiple squares are not considered
- ▶ Moving target t behind a square makes it relevant



RayScan Concepts

Skipped Successors

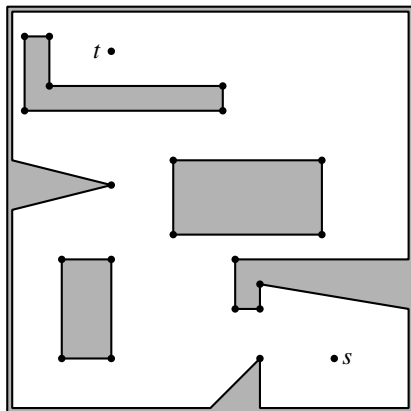
- ▶ Multiple squares are not considered
- ▶ Moving target t behind a square makes it relevant
- ▶ Since rays direct the search, this reduces the successors and number of rays shot



Comparisons to Visibility Graphs

RayScan

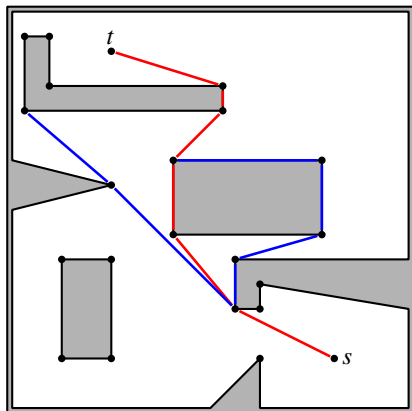
- ▶ Applying RayScan to a larger scenario



Comparisons to Visibility Graphs

RayScan

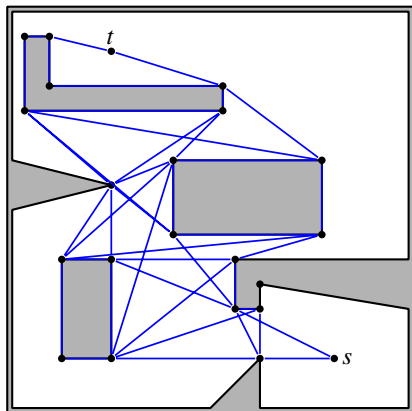
- ▶ Applying RayScan to a larger scenario
- ▶ Diagram shows RayScan search successors



Comparisons to Visibility Graphs

Sparse Visibility Graph

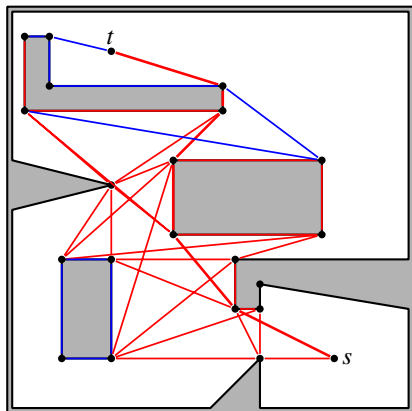
- ▶ Blue lines show the edges of the sparse visibility graph



Comparisons to Visibility Graphs

Sparse Visibility Graph

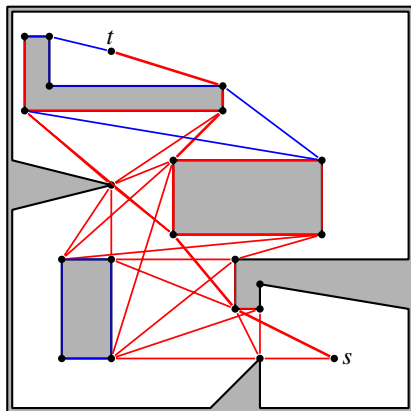
- ▶ Blue lines show the edges of the sparse visibility graph
- ▶ Red lines show the edges expanded during an A* search



Comparisons to Visibility Graphs

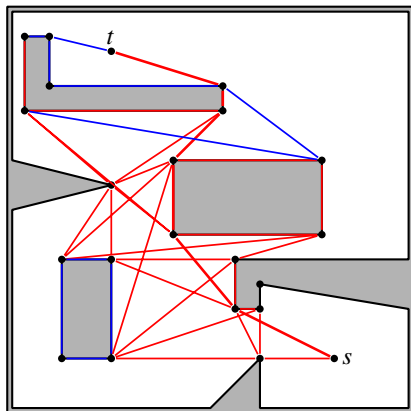
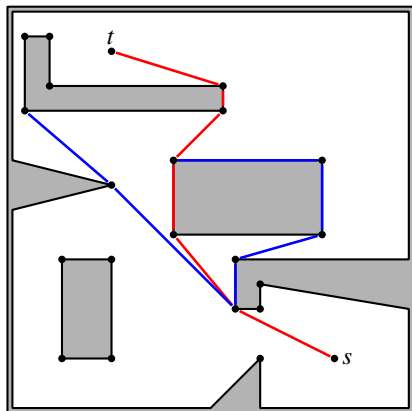
Sparse Visibility Graph

- ▶ Blue lines show the edges of the sparse visibility graph
- ▶ Red lines show the edges expanded during an A* search
- ▶ RayScan generates edges found on the sparse visibility graphs on-the-fly



Comparisons to Visibility Graphs

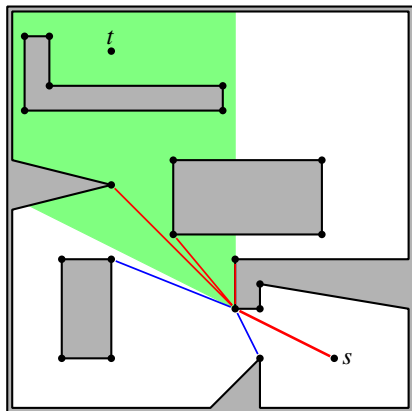
Sparse Visibility Graph Compare



Comparisons to Visibility Graphs

Visibility Graph with Projection Field

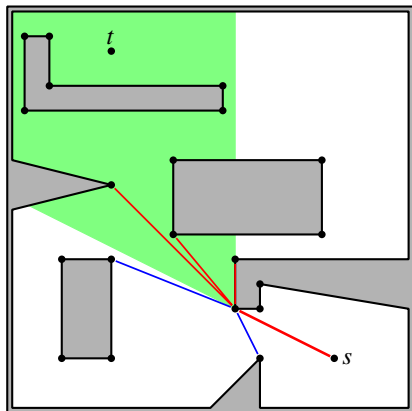
- ▶ The projection field concept can be applied to visibility graph on A^*



Comparisons to Visibility Graphs

Visibility Graph with Projection Field

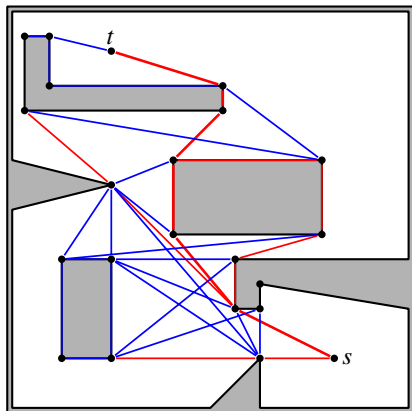
- ▶ The projection field concept can be applied to visibility graph on A^*
- ▶ Add only the successors of A^* within the projection field



Comparisons to Visibility Graphs

Visibility Graph with Projection Field

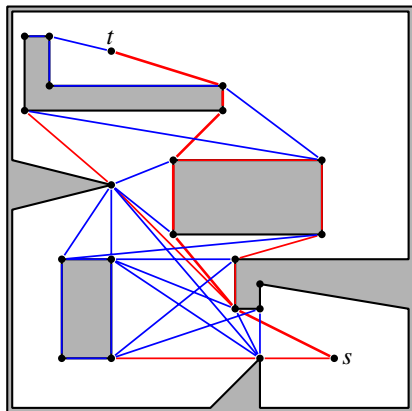
- ▶ The projection field concept can be applied to visibility graph on A^*
- ▶ Add only the successors of A^* within the projection field
- ▶ The search proceeds similarly to RayScan with this change



Comparisons to Visibility Graphs

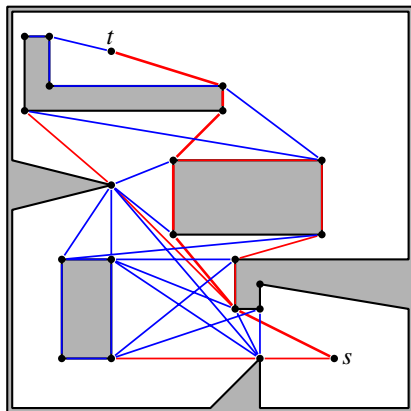
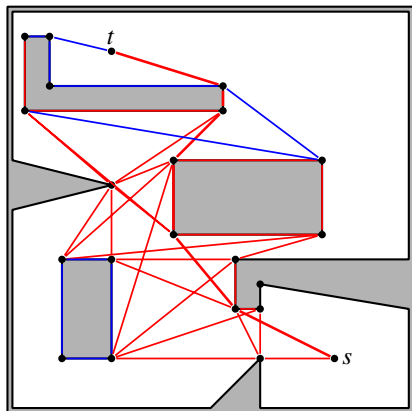
Visibility Graph with Projection Field

- ▶ The projection field concept can be applied to visibility graph on A^*
- ▶ Add only the successors of A^* within the projection field
- ▶ The search proceeds similarly to RayScan with this change
- ▶ This is referred as taut A^* by Oh et al. (2017)



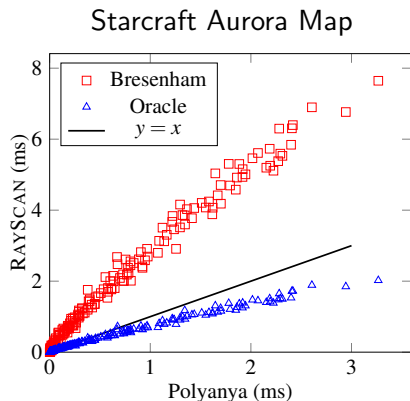
Comparisons to Visibility Graphs

Visibility Graph with Projection Field Compare



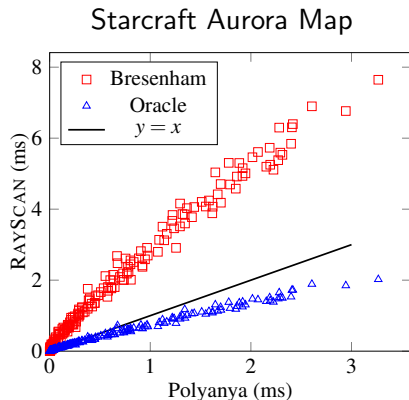
Results Presented in Paper

- ▶ Testing against Moving AI Lab pathfinding benchmarks (Sturtevant 2012)



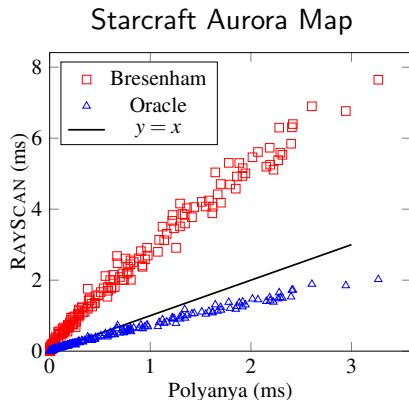
Results Presented in Paper

- ▶ Testing against Moving AI Lab pathfinding benchmarks (Sturtevant 2012)
- ▶ Comparing RayScan against Polyanya



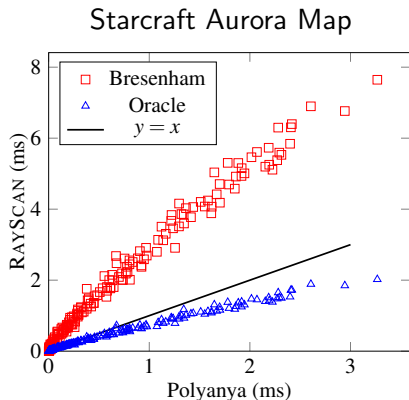
Results Presented in Paper

- ▶ Testing against Moving AI Lab pathfinding benchmarks (Sturtevant 2012)
- ▶ Comparing RayScan against Polyanya
- ▶ Bresenham is RayScan using a Bresenham line for the ray shooting (Bresenham 1965)



Results Presented in Paper

- ▶ Testing against Moving AI Lab pathfinding benchmarks (Sturtevant 2012)
- ▶ Comparing RayScan against Polyanya
- ▶ Bresenham is RayScan using a Bresenham line for the ray shooting (Bresenham 1965)
- ▶ Oracle uses a free ray shooter



Recap

- ▶ RayScan works directly on the environment

Recap

- ▶ RayScan works directly on the environment
- ▶ Well suited to single instance or dynamically changing maps

Recap

- ▶ RayScan works directly on the environment
- ▶ Well suited to single instance or dynamically changing maps
- ▶ Performance dependent on ray shooter (i.e. more than half runtime is shooting rays)

References

- Lozano-Pérez, T., & Wesley, M. A. (1979). An algorithm for planning collision-free paths among polyhedral obstacles. *Communications of the ACM*, 22(10), 560–570.
- Oh, S., & Leong, H. W. (2017). Edge n-level sparse visibility graphs: Fast optimal any-angle pathfinding using hierarchical taut paths. *Proceedings of the Tenth International Symposium on Combinatorial Search (SoCS 2017)*.
- Cui, M. L., Harabor, D., & Grastien, A. (2017). Compromise-free pathfinding on a navigation mesh. *Proceedings of the 26th International Joint Conference on Artificial Intelligence*, 496–502.
- Sturtevant, N. (2012). Benchmarks for grid-based pathfinding. *Transactions on Computational Intelligence and AI in Games*, 4(2), 144–148.
<http://web.cs.du.edu/~sturtevant/papers/benchmarks.pdf>
- Bresenham, J. E. (1965). Algorithm for computer control of a digital plotter. *IBM Systems journal*, 4(1), 25–30.